

R Short Course: Day 5

Using R in the classroom
Programming in R

Programming in R

I. Data types

II. operators

III. simple functions

IV. Writing functions

Data structures

- I. elements: logical, integer, real, character, factor
- II. vectors: ordered sets of elements of one type
- III. matrices: ordered sets of vectors (all of one type)
- IV. data.frames: ordered sets of vectors, may be different types
- V. lists: ordered set of anything

Operators

I. arithmetical

1. +, -, *, /, ^, %%

2. a + b, a-b, a*b, a/b, a^b, a %%b

II. Logical

A. ==, !, !=, >, <, >=, <=

III. Matrix

A. %*% is matrix multiplication

B. %o% is outer product

```
> a <- 2
> b <- 3
> v <- 5:10
> w <- 6:7
> v
[1] 5 6 7 8 9 10
> w
[1] 6 7
> v ^a
[1] 25 36 49 64 81 100
> w* b
[1] 18 21
> w * v
[1] 30 42 42 56 54 70
```

example operations

Matrix operations

```
> v
[1] 5 6 7 8 9 10
> t(v)
[,1] [,2] [,3] [,4] [,5] [,6]
[1,] 5 6 7 8 9 10
> t(v) %*% v
[,1]
[1,] 355
> v %*% t(v)
[,1] [,2] [,3] [,4] [,5] [,6]
[1,] 25 30 35 40 45 50
[2,] 30 36 42 48 54 60
[3,] 35 42 49 56 63 70
[4,] 40 48 56 64 72 80
[5,] 45 54 63 72 81 90
[6,] 50 60 70 80 90 100
```

Additional matrix operators

outer product

```
> v
[1] 5 6 7 8 9 10
> w
[1] 6 7
> v %o% w
     [,1] [,2]
[1,]   30   35
[2,]   36   42
[3,]   42   49
[4,]   48   56
[5,]   54   63
[6,]   60   70
```

matrix “addition” (psych)

```
> x <- seq(4,8,2)
> x
[1] 4 6 8
> x %+% t(x)
     [,1] [,2] [,3]
[1,]    8   10   12
[2,]   10   12   14
[3,]   12   14   16
```

Review of Matrix Algebra

I. scalers, vectors, and matrices

A.scalers: simple numbers

B.vectors: ordered sets of numbers

1. $V1 = \{1 2 3 4 5 6 7 8 9 10\}$
2. $V2 = \{11 12 13 14 15 16 17 18 19 20\}$
3. $V2[3] = 13$

C.Matrices (vectors of vectors)

See personality-project.org/r/sem.appendix.I.pdf

Matrices

$$n \times m = \left\{ \begin{array}{l} X_{11} X_{12} \dots X_{1m} \\ X_{21} X_{22} \dots X_{2m} \\ \dots \dots \dots \\ X_{n1} X_{n2} \dots X_{nm} \end{array} \right\}$$

$$\begin{matrix} R \\ \begin{matrix} & x_1 & x_2 & x_3 \\ x_1 & 1.00 & 0.56 & 0.48 \\ x_2 & 0.56 & 1.00 & 0.42 \\ x_3 & 0.48 & 0.42 & 1.00 \end{matrix} \end{matrix}$$

X _{ij}	V1	V2	V3	V4
S1	9	4	9	7
S2	9	7	1	8
S3	2	9	9	3
S4	8	2	9	6
S5	6	4	0	0
S6	5	9	5	8
S7	7	9	3	0
S8	1	1	9	2
S9	6	4	4	9
S10	7	5	8	6

Vector operations

I. addition

A. $V3 <- V1 + V2$

B. $V3 = \{12 14 16 18 20 22 24 26 28 30\}$

II. multiplication

A. element by element

$$1. V1 * V2 = 11 24 39 56 75 96 119 144 171 200$$

B. inner product of vector (Sums of products)

C. outer product of vectors (matrix of products)

Inner and outer products

$$inner.product = \sum_{i=1}^N V1_i * V2_i$$

$$_nX_1 *_1 Y_m =_n (XY)_m$$

Outer product (graphically)

```
> V1  
  
[1] 1 2 3 4 5 6 7 8 9 10  
  
> V2  
  
[1] 1 2 3 4  
  
> outer.prod <- V1 %*% t(V2)  
> outer.prod  
  
[,1] [,2] [,3] [,4]  
[1,] 1 2 3 4  
[2,] 2 4 6 8  
[3,] 3 6 9 12  
[4,] 4 8 12 16  
[5,] 5 10 15 20  
[6,] 6 12 18 24  
[7,] 7 14 21 28  
[8,] 8 16 24 32  
[9,] 9 18 27 36  
[10,] 10 20 30 40
```

Matrix Operations

I. Addition/Subtraction

A. (element by element)

B.must be of same dimensions

II.Multiplication

A. $mX_n \cdot nY_p = mXY_p$ where the elements of XY , x_{ij} are the sums of the products of the elements of the i th row and j th column

B. $X Y \neq Y X$

Matrix multiplication

$$mX_n \cdot nY_p = mXY_p$$

$$xY_{ij} = \sum_{k=1}^N x_{ik} * y_{jk}.$$

Matrix multiplication for data

one	X _{ij}			
1 1 1 1 1 1 1 1 1 1	V1	V2	V3	V4
one %*% Xij=	S1	9	4	9
V1 V2 V3 V4	S2	9	7	1
[1,] 60 54 57 49	S3	2	9	9
	S4	8	2	9
	S5	6	4	0
	S6	5	9	5
X.means <- one %*% Xij/n	S7	7	9	3
V1 V2 V3 V4	S8	1	1	9
[1,] 6 5.4 5.7 4.9	S9	6	4	4
	S10	7	5	8
				6

Deviation scores as matrix differences

```
X.diff <- Xij - one %*% X.means
```

	V1	V2	V3	V4
S1	3	-1.4	3.3	2.1
S2	3	1.6	-4.7	3.1
S3	-4	3.6	3.3	-1.9
S4	2	-3.4	3.3	1.1
S5	0	-1.4	-5.7	-4.9
S6	-1	3.6	-0.7	3.1
S7	1	3.6	-2.7	-4.9
S8	-5	-4.4	3.3	-2.9
S9	0	-1.4	-1.7	4.1
S10	1	-0.4	2.3	1.1

Covariance as matrix product

```
X.cov <- t(X.diff) %*% X.diff/(n - 1)
```

```
X.cov
```

	V1	V2	V3	V4
V1	7.33	0.11	-3.00	3.67
V2	0.11	8.71	-3.20	-0.18
V3	-3.00	-3.20	12.68	1.63
V4	3.67	-0.18	1.63	11.43

```
diag(X.cov)
```

	V1	V2	V3	V4
V1	7.33	8.71	12.68	11.43

Correlation = standardized covariance

	V1	V2	V3	V4
V1	0.37	0.00	0.00	0.0
V2	0.00	0.34	0.00	0.0
V3	0.00	0.00	0.28	0.0
V4	0.00	0.00	0.00	0.3

```
sdi <-  
diag(1/sqrt(diag(X.cov)))
```

	V1	V2	V3	V4
V1	1.00	0.01	-0.31	0.40
V2	0.01	1.00	-0.30	-0.02
V3	-0.31	-0.30	1.00	0.14
V4	0.40	-0.02	0.14	1.00

```
X.cor <-  
sdi %*% X.cov %*% sdi
```

The identity matrix

```
I <- diag(1,nrow=4)
```

	[,1]	[,2]	[,3]	[,4]
[1,]	1	0	0	0
[2,]	0	1	0	0
[3,]	0	0	1	0
[4,]	0	0	0	1

Matrix Inverse

$$X'X^{-1} = X^{-1}X = I$$

	V1	V2	V3	V4
V1	1.00	0.01	-0.31	0.40
V2	0.01	1.00	-0.30	-0.02
V3	-0.31	-0.30	1.00	0.14
V4	0.40	-0.02	0.14	1.00

X.cor

	V1	V2	V3	V4
V1	1.44	0.15	0.58	-0.65
V2	0.15	1.12	0.40	-0.09
V3	0.58	0.40	1.36	-0.41
V4	-0.65	-0.09	-0.41	1.32

X.cor⁻¹

$$X^{-1}X = XX^{-1} = I$$

X.inv %*% X.cor

	V1	V2	V3	V4
V1	1	0	0	0
V2	0	1	0	0
V3	0	0	1	0
V4	0	0	0	1

X.cor %*% X.inv

	V1	V2	V3	V4
V1	1	0	0	0
V2	0	1	0	0
V3	0	0	1	0
V4	0	0	0	1

Matrix algebra is your friend

Functions

- I. Operate on an object and provide a new object
- II. e.g., `f <- function(x) {x * 2}`

```
> f <- function(x) {x * 2}  
> f(43)  
[1] 86  
> x  
[1] 4 6 8  
> f(x)  
[1] 8 12 16  
> f(v %o% w)  
      [,1] [,2]  
[1,]    60   70  
[2,]    72   84  
[3,]    84   98  
[4,]    96  112  
[5,]   108  126  
[6,]   120  140
```

Simple functions

a subset of useful functions

- I. `is.na()`, `is.null()`, `is.vector()`, `is.matrix()`,
`is.list()`
- II. `sum()`, `rowSums()`, `colSums()`, `mean(x)`,
`rowMeans()`, `colMeans()`, `max`, `min`, `median`
(these work on the entire matrix)
- III. `var`, `cov`, `cor`, `sd` (these work on the columns
of the matrix/`data.frame`)
- IV. `help.start()` brings up a web page of manuals

More useful functions

I. `rep(x,n)` (repeats the value x n times)

II. `c(x,y)` (combines x with y)

III. `cbind(x,y)` combines column wise

IV. `rbind(x,y)` combines rowwise

V. `seq(a,b,c)` sequence from a to b stepping
by c

sums on matrices and data.frames

```
> z <- f( v %o% w)
> z
      [,1] [,2]
[1,]    60   70
[2,]    72   84
[3,]    84   98
[4,]    96  112
[5,]   108  126
[6,]   120  140

> rowSums(z)
[1] 130 156 182 208 234 260
> colSums(z)
[1] 540 630
> mean(z)
[1] 97.5
> rowMeans(z)
[1] 65 78 91 104 117 130
> median(z)
[1] 97
```

```
> var(z)
      [,1] [,2]
[1,] 504 588
[2,] 588 686
> cov(z)
      [,1] [,2]
[1,] 504 588
[2,] 588 686
> cor(z)
      [,1] [,2]
[1,]    1    1
[2,]    1    1
> sd(z)
[1] 22.44994 26.19160
> z
      [,1] [,2]
[1,]   60   70
[2,]   72   84
[3,]   84   98
[4,]   96  112
[5,]  108  126
[6,]  120  140
```

Basic stats functions, part 2

?cor

```
var(x, y = NULL, na.rm = FALSE, use)

cov(x, y = NULL, use = "everything",
     method = c("pearson", "kendall",
"spearmann"))

cor(x, y = NULL, use = "everything",
     method = c("pearson", "kendall",
"spearmann"))

cov2cor(V)
```

More on cor

x

a numeric vector, matrix or data frame.

y

NULL (default) or a vector, matrix or data frame with compatible dimensions to x. The default is equivalent to y = x (but more efficient).

na.rm

logical. Should missing values be removed?

use

an optional character string giving a method for computing covariances in the presence of missing values. This must be (an abbreviation of) one of the strings "everything", "all.obs", "complete.obs", "na.or.complete", or "pairwise.complete.obs".

method

a character string indicating which correlation coefficient (or covariance) is to be computed. One of "pearson" (default), "kendall", or "spearman", can be abbreviated.

v

symmetric numeric matrix, usually positive definite such as a covariance matrix.

row and col as functions

```
> r <- .8
> R <- diag(1,8)
> R
      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
[1,]    1    0    0    0    0    0    0    0
[2,]    0    1    0    0    0    0    0    0
[3,]    0    0    1    0    0    0    0    0
[4,]    0    0    0    1    0    0    0    0
[5,]    0    0    0    0    1    0    0    0
[6,]    0    0    0    0    0    1    0    0
[7,]    0    0    0    0    0    0    1    0
[8,]    0    0    0    0    0    0    0    1
> R <- r^(abs(row(R)-col(R)))
> round(R,2)
      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
[1,] 1.00  0.80  0.64  0.51  0.41  0.33  0.26  0.21
[2,] 0.80  1.00  0.80  0.64  0.51  0.41  0.33  0.26
[3,] 0.64  0.80  1.00  0.80  0.64  0.51  0.41  0.33
[4,] 0.51  0.64  0.80  1.00  0.80  0.64  0.51  0.41
[5,] 0.41  0.51  0.64  0.80  1.00  0.80  0.64  0.51
[6,] 0.33  0.41  0.51  0.64  0.80  1.00  0.80  0.64
[7,] 0.26  0.33  0.41  0.51  0.64  0.80  1.00  0.80
[8,] 0.21  0.26  0.33  0.41  0.51  0.64  0.80  1.00
```

Yet more stats functions

- I. `sample(n, N, replace=TRUE)`
- II. `eigen(X)` (eigen value decomposition of X)
- III. `solve(X)` (inverse of X)
- IV. `solve (X,Y)` Regression of Y on X

```
> x <- matrix(sample(10,50,replace=TRUE),ncol=5)
> x
```

	[,1]	[,2]	[,3]	[,4]	[,5]
[1,]	10	3	4	4	6
[2,]	3	10	8	8	9
[3,]	1	6	5	8	5
[4,]	9	1	3	5	3
[5,]	6	8	3	5	1
[6,]	8	6	10	1	10
[7,]	10	5	10	2	1
[8,]	9	3	2	2	9
[9,]	6	10	2	9	4
[10,]	1	8	8	2	6

Creating a matrix

```
> z <- scale(x)
```

standardize it

```
> z
      [,1]      [,2]      [,3]      [,4]      [,5]
[1,]  1.04838349 -0.9819805 -0.4678877 -0.2059329  0.1852621
[2,] -0.93504473  1.3093073  0.7798129  1.1669533  1.1115724
[3,] -1.50173851  0.0000000 -0.1559626  1.1669533 -0.1235080
...
[9,] -0.08500407  1.3093073 -1.0917380  1.5101749 -0.4322782
[10,] -1.50173851  0.6546537  0.7798129 -0.8923761  0.1852621
attr("scaled:center")
[1] 6.3 6.0 5.5 4.6 5.4
attr("scaled:scale")
[1] 3.529243 3.055050 3.205897 2.913570 3.238655
```

Just center it

```
> c <- scale(x,scale=FALSE)

> c
     [,1] [,2] [,3] [,4] [,5]
[1,]  3.7   -3  -1.5 -0.6  0.6
[2,] -3.3    4   2.5  3.4  3.6
[3,] -5.3    0  -0.5  3.4 -0.4
[4,]  2.7   -5  -2.5  0.4 -2.4
[5,] -0.3    2  -2.5  0.4 -4.4
[6,]  1.7    0   4.5 -3.6  4.6
[7,]  3.7   -1   4.5 -2.6 -4.4
[8,]  2.7   -3  -3.5 -2.6  3.6
[9,] -0.3    4  -3.5  4.4 -1.4
[10,] -5.3   2   2.5 -2.6  0.6
attr(,"scaled:center")
[1] 6.3 6.0 5.5 4.6 5.4
```

Find the covariance and inverse

```
> c <- cov(x)
> round(c,2)
      [,1]   [,2]   [,3]   [,4]   [,5]
[1,] 12.46 -6.89 -1.61 -4.53 -1.58
[2,] -6.89  9.33  2.11  4.11  0.56
[3,] -1.61  2.11 10.28 -3.89  2.22
[4,] -4.53  4.11 -3.89  8.49 -1.60
[5,] -1.58  0.56  2.22 -1.60 10.49

> round(solve(c),2)
      [,1]   [,2]   [,3]   [,4]   [,5]
[1,] 0.15  0.08  0.02  0.06  0.02
[2,] 0.08  0.23 -0.07 -0.10  0.00
[3,] 0.02 -0.07  0.16  0.12 -0.01
[4,] 0.06 -0.10  0.12  0.26  0.03
[5,] 0.02  0.00 -0.01  0.03  0.10
```

Flow control

I. if(condition) {then do this} else {do this}

II. for (condition) do {expression}

A. for (i in 1:n) do {x <- x + 1}

III. while (condition) {expression}

conditionals

I. (a & b) vs. (a && b)

II. (a | b) vs. (a || b)

```
a <- 1
> if (a & b) {print ("hello")} else {print("goodby")}
Error: object 'b' not found
> if (a && b ) {print ("hello")} else {print("goodby")}
[1] "goodby"
> if (a | b) {print ("hello")} else {print("goodby")}
Error: object 'b' not found

> if (a || b) {print ("hello")} else {print("goodby")}
Error: object 'b' not found
> a <- 1
> if (a || b) {print ("hello")} else {print("goodby")}
[1] "hello"
>
```

simple control

```
> a <- 1
> b <- 2
> c <- 3
> k <- 10
> x <- 1
> if(x == a) {print("x is the same as a and has
value",x)} else {print ("x is not equal to a")}

> x <- 3
> if(x == a) {print("x is the same as a and has
value",x)} else {print ("x is not equal to a")}
[1] "x is not equal to a"
>
```

Make that a function

```
> f1 <- function(x,y) {if(x == y)
{print("x is the same as y and has
value",x)} else {print ("x is not equal
to y")}}
> f1(3,4)
[1] "x is not equal to y"
> f1(5,5)
[1] "x is the same as y and has value"
```

Simple functions:part 2

- I. Find the squared multiple correlation of a variable with all the other variables in a matrix.
- II. The R^2 is 1- the residual variance

The essence of the function

```
SMC <- function(R) {  
  R.inv <- solve(R)  
  SMC <- 1 - 1/diag(R.inv)}  
  
> S <- cor(attitude)  
> SMC(S)      #does not show anything  
  
> round(SMC(S),2) #but this does  
                  rating complaints privileges learning      raises  
critical          advance  
                 0.73          0.77          0.38          0.62          0.68  
0.19          0.52
```

Add a return

```
SMC <- function(R) {  
  R.inv <- solve(R)  
  SMC <- 1 - 1/diag(R.inv)  
  return(SMC)}  
  
> SMC(S)  
    rating complaints privileges learning      raises  
critical      advance  
 0.7326020  0.7700868  0.3831176  0.6194561  0.6770498  
0.1881465  0.5186447
```

Allow it to find R

```
SMC <- function(R) {  
  if(dim(R)[1] !=dim(R)[2]) {R <-cor(R)}  
  R.inv <- solve(R)  
  SMC <- 1 - 1/diag(R.inv)  
  return(SMC)}
```

```
> SMC(attitude)  
    rating complaints privileges   learning      raises  
critical       advance  
 0.7326020  0.7700868  0.3831176  0.6194561  0.6770498  
0.1881465  0.5186447
```

Clean up the output

```
SMC <- function(R,digits=2) {  
  if(dim(R)[1] !=dim(R)[2]) {R <- cor(R)}  
  R.inv <- solve(R)  
  SMC <- 1 - 1/diag(R.inv)  
  return(round(SMC,digits))}  
  
> SMC(attitude)  
    rating complaints privileges learning      raises critical  
advance  
       0.73        0.77       0.38       0.62       0.68      0.19  
0.52  
>
```

Check for poor input

```
> att <- data.frame(attitude[1:3],attitude[1:3])
> SMC(att)
Error in solve.default(R) :
  Lapack routine dgesv: system is exactly singular
```

Add checks for weird matrices

```
SMC <- function(R,digits=2) {  
  p <- dim(R)[2]  
  if (dim(R)[1] != p) {R <- cor(R)}  
  R.inv <- try(solve(R),TRUE)  
  if(class(R.inv)== as.character("try-error")) {SMC <- rep(1,p)  
    warning("Correlation matrix not invertible, smc's returned as 1s")}  
  else {smc <- 1 - 1/diag(R.inv)}  
  SMC <- 1 - 1/diag(R.inv)}  
  return(round(SMC,digits))}  
  
> SMC(att)  
[1] 1 1 1 1 1 1  
Warning message:  
In SMC(att) : Correlation matrix not invertible, smc's returned as  
1s  
  
> SMC(attitude)  
      rating complaints privileges learning      raises critical  
       0.73          0.77         0.38        0.62        0.68        0.19
```

Further checks

Input is a covariance matrix

```
> SMC(cov(attitude))
    rating complaints privileges learning      raises   critical
advance
-38.62       -39.76      -91.35     -51.42      -33.91     -78.49
-49.96
```

Input is raw data or correlations

```
> SMC(cor(attitude))
    rating complaints privileges learning      raises   critical
advance
  0.73        0.77        0.38       0.62       0.68       0.19
  0.52
> SMC(attitude)
    rating complaints privileges learning      raises   critical
advance
  0.73        0.77        0.38       0.62       0.68       0.19
  0.52
```

Final version

```
#modified Dec 10, 2008 to return 1 on diagonal if non-invertible
#modified March 20, 2009 to return smcs * variance if covariance matrix
is desired
#modified April 8, 2009 to remove bug introduced March 10 when using
covar from data
"smc" <-
function(R,covar =FALSE) {
failed=FALSE
p <- dim(R)[2]
if (dim(R)[1] != p) {if(covar) {C <- cov(R, use="pairwise")
vari <- diag(C)
R <- cov2cor(C)
} else {R <- cor(R,use="pairwise")}}
else {vari <- diag(R)
R <- cov2cor(R)
if (!is.matrix(R)) R <- as.matrix(R)}
R.inv <- try(solve(R),TRUE)
if(class(R.inv)== as.character("try-error")) {smc <- rep(1,p)
warning("Correlation matrix not invertible, smc's returned as 1s")}
else {smc <- 1 -1/diag(R.inv)
if(covar) {smc <- smc * vari}}
return(smc)
}
```

Creating a new function

- I. Is there a base function to modify?
- II. Consider the case of modifying Promax rotation to allow for any target matrix
- III. original promax (inside the factanal package) had been modified to report the factor correlation.
- IV. This version was created with the assistance of Pat Shrout and Steve Miller

promax

```
> promax
function (x, m = 4)
{
  if (ncol(x) < 2)
    return(x)
  dn <- dimnames(x)
  xx <- varimax(x)
  x <- xx$loadings
  Q <- x * abs(x)^(m - 1)
  U <- lm.fit(x, Q)$coefficients
  d <- diag(solve(t(U) %*% U))
  U <- U %*% diag(sqrt(d))
  dimnames(U) <- NULL
  z <- x %*% U
  U <- xx$rotmat %*% U
  dimnames(z) <- dn
  class(z) <- "loadings"
  list(loadings = z, rotmat = U)
}
<environment: namespace:stats>
```

```
> Promax
function (x, m = 4)
{
  if (!is.matrix(x) & !is.data.frame(x)) {
    if (!is.null(x$loadings))
      x <- as.matrix(x$loadings)
  }
  else {
    x <- x
  }
  if (ncol(x) < 2)
    return(x)
  dn <- dimnames(x)
  xx <- varimax(x)
  x <- xx$loadings
  Q <- x * abs(x)^(m - 1)
  U <- lm.fit(x, Q)$coefficients
  d <- diag(solve(t(U) %*% U))
  U <- U %*% diag(sqrt(d))
  dimnames(U) <- NULL
  z <- x %*% U
  U <- xx$rotmat %*% U
  ui <- solve(U)
  Phi <- ui %*% t(ui)
  dimnames(z) <- dn
  class(z) <- "loadings"
  result <- list(loadings = z, rotmat = U, Phi = Phi)
  class(result) <- c("psych", "fa")
  return(result)}
```

Promax

```
"target.rot" <-
function (x, keys=NULL,m = 4)
{
  if(!is.matrix(x) & !is.data.frame(x) )  {
    if(!is.null(x$loadings)) x <- as.matrix(x$loadings)
  } else {x <- x}
  if (ncol(x) < 2)
    return(x)
  dn <- dimnames(x)
  if(is.null(keys)) {xx <- varimax(x)
  x <- xx$loadings
  Q <- x * abs(x)^(m - 1)} else {Q <- keys}
  U <- lm.fit(x, Q)$coefficients
  d <- diag(solve(t(U) %*% U))
  U <- U %*% diag(sqrt(d))
  dimnames(U) <- NULL
  z <- x %*% U
  if (is.null(keys)) {U <- xx$rotmat %*% U } else {U <- U}
  ui <- solve(U)
  Phi <- ui %*% t(ui)
  dimnames(z) <- dn
  class(z) <- "loadings"
  result <- list(loadings = z, rotmat = U,Phi = Phi)
  class(result) <- c("psych","fa")
  return(result)
}
```

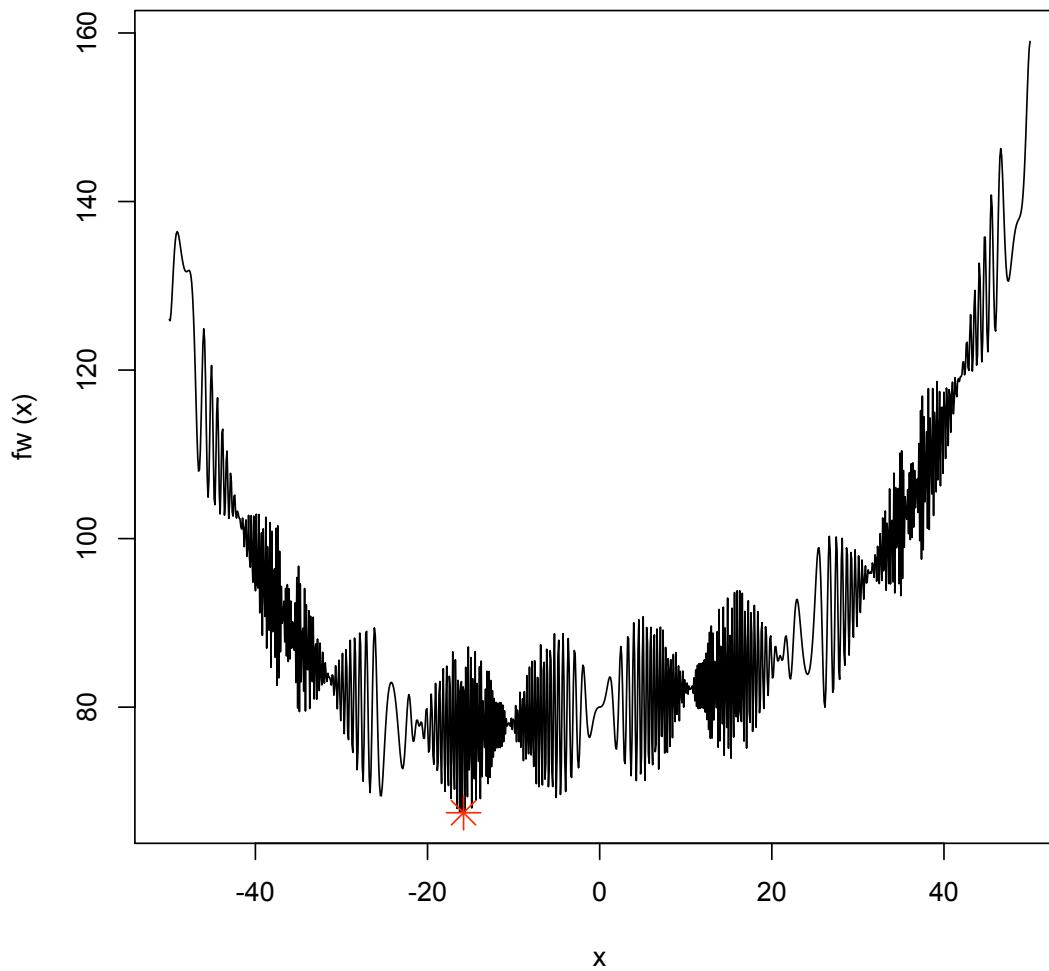
target.rot

optim as “solver” for R

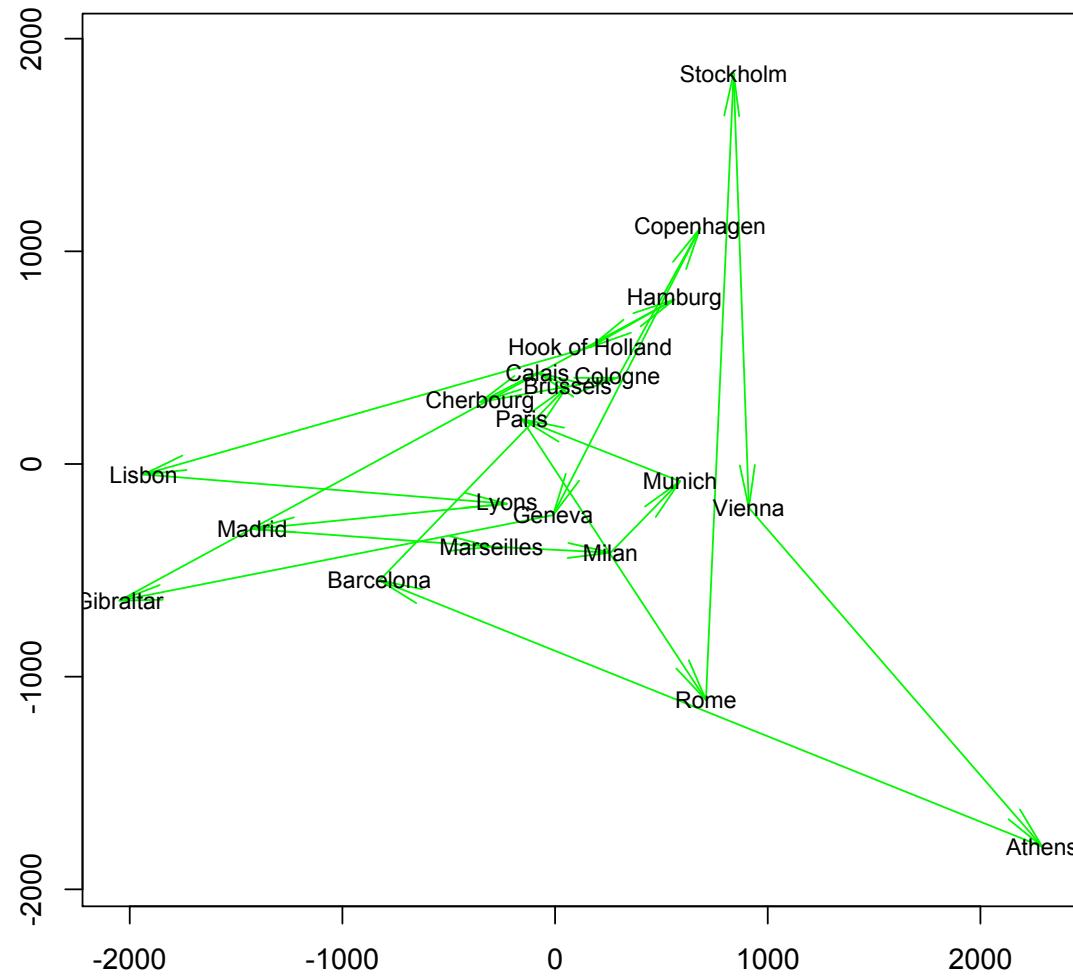
- I. Many statistical functions are not closed form but rather are solved iteratively.
- II. We start with a good guess and then minimize the function
- III. optim will do this for functions where you manipulate one vector (which can of course actually be a matrix)

optim

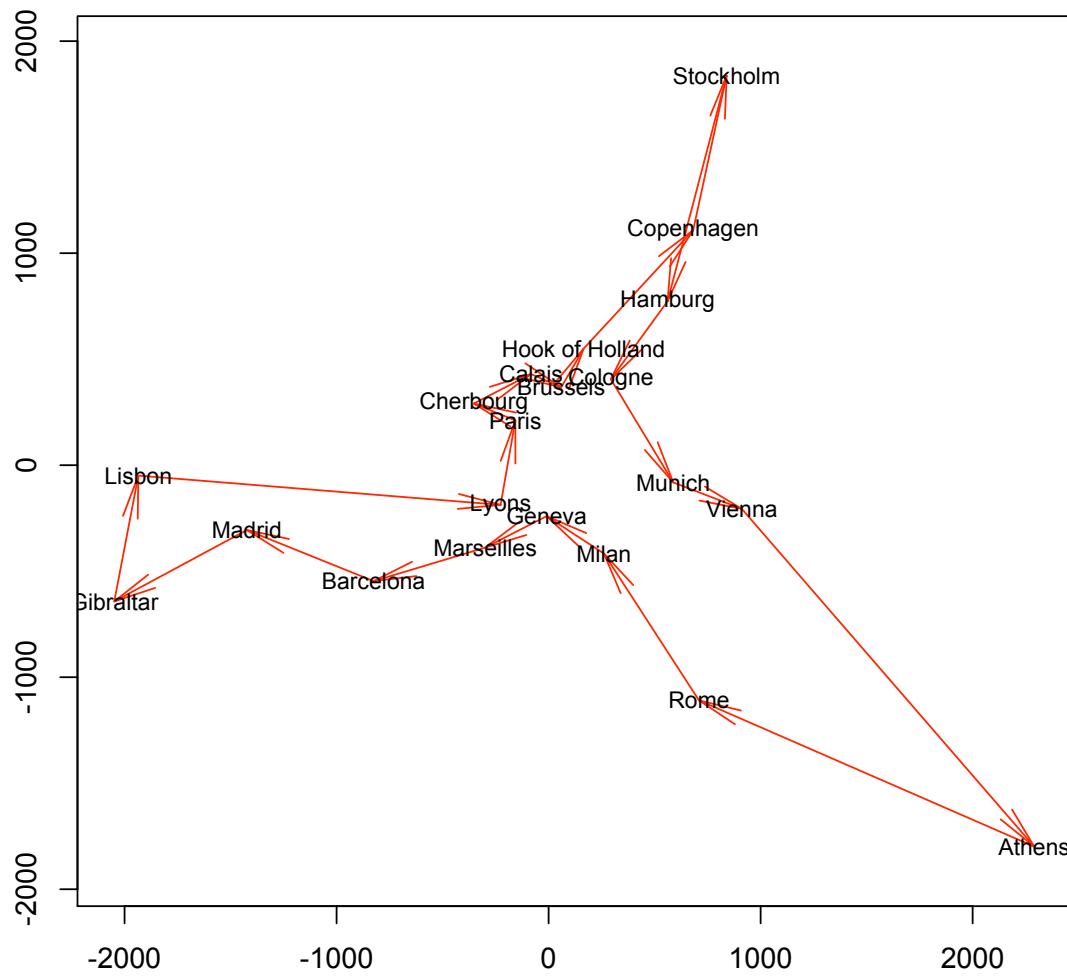
optim() minimising 'wild function'



initial solution of traveling salesman problem



optim() 'solving' traveling salesman problem



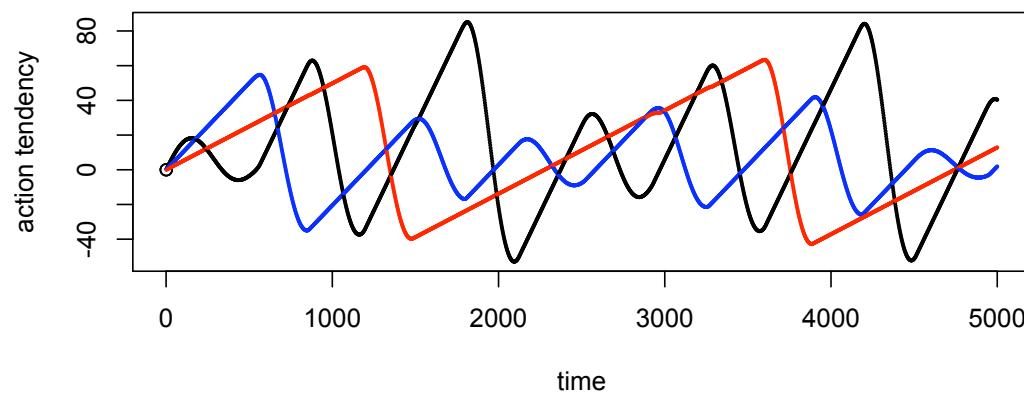
Trying to make a new function to do OLS FA

- I. First, look at current ML FA function
 - A. factanal
 - B. It turns out that the critical optimization is done in factanal.fit.mle, but where is that?
- II. getAnywhere(factanal.fit.mle)
 - A. then look at the code
 - B. scratch your head and try running it

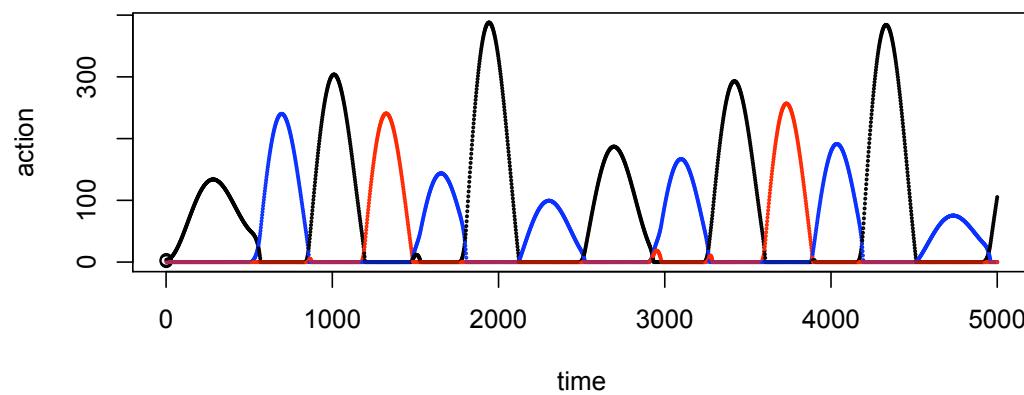
R in the classroom

- I. Undergraduate statistics and research methods
 - A.describe, pairs.panels, anova, lm
 - B.plot, curve, etc.
 - C.see tutorials for 205 and 371
 - D.simulations of data for simulated studies
 - E.Examples of complex models

Action Tendencies over time



Actions over time



R in the classroom

I. Graduate

- A. data simulations
- B. data analysis
- C. longer tutorial