Psychology 205: Research Methods in Psychology The problem of base rates

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Outline

Inferential statistics

The problem of base rates

Hypothesis testing using inferential statistics

- How likely are the observed data given the hypothesis that an Independent Variable has no effect.
- Bayesian statistics compare the likelihood of the data given the hypothesis of no differences as contrasted to the likelihood of the data given competing hypotheses.
 - This takes into account our prior willingness to believe that the IV could have an effect.
 - Also takes into account our strength of belief in the hypothesis of no effect
- Conventional tests report the probability of the data given the "Null" hypothesis of no difference.
- The less likely the data are to be observed given the Null, the more we tend to discount the Null.
 - Three kinds of inferential errors: Type I, Type II and Type III
 - Type I is rejecting the Null when in fact it is true
 - Type II is failing to reject the Null when it is in fact not true
 - Type III is asking the wrong question

Hypothesis Testing

Table : The ways we can be mistaken

		State of the World		
		True False		
Scientists says	s True Valid Positi		Type I error	
	False	Type II error	Valid rejection	

Type III error is asking the wrong question!

Hypothesis Testing α and β

Table : The ways we can be mistaken

		State of the World			
		True False			
Scientists says	True	Valid Positive	(Type I error) = α		
	False	p(Type II error) = β	Valid rejection		

Power as 1- β We need to think about power. Type III error is asking the wrong question! Probability that a "significant effect" is a type I error = $\frac{\alpha * False}{\alpha * False + (1-\beta) * True}$

Consider a number of scenarios

- 1. 1000 studies all together
 - Consider $\alpha = .05, .01$
 - Consider $1 \beta = .5, .8, .95, 1.0$
- 2. But, also consider the state of the world (What is the a priori likelihood of the outcome)
 - a 50-50 chance (boring result)
 - a 20-80 chance (interesting finding)
 - a 10-90 chance (very interesting finding)
 - a 1-99 chance (Wow, you found that!)
- 3. Probability that a "significant effect" is a type I error = $\frac{\alpha * False}{\alpha * False + (1-\beta) * True}$

Hypothesis Testing α and β

Table : The ways we can be mistaken

		State of the World			
		True False			
Scientists says	True	$VP = (1-eta) * \mathit{True}$	$p(Type I) = \alpha * False$		
	False	$p(Type II) = \beta * True$	$VR = (1 - \alpha) * False$		

Power as 1- β We need to think about power. probability that a "significant effect" is a type I error = $\frac{\alpha * False}{\alpha * False + (1-\beta) * True}$

Hypothesis Testing α and β likely event, high power

Table : A 50 - 50 chance – high power

		State		
		True	False	Total
Scientists says	True	475	25	500
	False	25	475	500
	Total	500	500	1000

p (False Positive — finding was significant) = $\frac{25}{25+475}$ = .05

Hypothesis Testing α and β likely event, 50% power

Table : A 50 - 50 chance - low power

		State		
		True	False	Total
Scientists says	True	250	25	275
	False	250	475	725
	Total	500	500	1000

p (False Positive — finding was significant) = $\frac{25}{25+250}$ = .09

Hypothesis Testing α and β unlikely event, 50% power

Table : A 10 - 90 chance - low power

		State		
		True	False	Total
Scientists says	True	50	45	95
	False	50	855	905
	Total	100	900	1000

p (False Positive — finding was significant) = $\frac{45}{45+50}$ = .47

Hypothesis Testing α and β very unlikely event, 80% power

Table : A 1 - 99 chance - good power

		State		
		True	False	Total
Scientists says	True	8	49.5	57.5
	False	2	940.5	942.5
	Total	10	990	1000

p (False Positive — finding was significant) = $\frac{49.5}{49.5+8}$ = .86

Hypothesis Testing α and β very unlikely event, perfect power

Table : A 1 - 99 chance - perfect power

		State		
		True	False	Total
Scientists says	True	10	49.5	59.5
	False	0	940.5	94.5
	Total	10	990	1000

p (False Positive — finding was significant) = $\frac{49.5}{49.5+10}$ = .83

Power, α level, and the excitement of the finding

- 1. There is a natural tendency to want to show the unlikely.
 - Showing your grandmother is right is not as interesting as showing she is wrong
 - Showing that what most people expect is wrong is very exciting
- 2. But, the less likely the effect is to be there, the more likely that a "significant effect" is actually a type I error.
 - Need to increase our Power and be sensitive to the replicability of our results.
- 3. The power of a good graphic to show the problem.
 - Five lines: *alpha* = .05, .01, .001
 - Power = .8 or 1

